

## Systems of Equations in Two Variables

Solve the system:  $3x + y = 20$   
 $2x + 3y = 18$

### Solve using Substitution:

- 1) Isolate one variable  
 $3x + y = 20$   
 $- 3x \quad - 3x$   
 $y = 20 - 3x$
- 2) Use this expression in place of the variable in the other equation and solve.  
 $2x + 3y = 18$   
 $2x + 3(20 - 3x) = 18$   
 $2x + 60 - 9x = 18$   
 $60 - 7x = 18$   
 $- 60 \quad - 60$   
 $\frac{-7x}{-7} = \frac{-42}{-7} \quad \boxed{x = 6}$
- 3) Use this solution in one of the original equations and solve for the other variable.  
 $3x + y = 20$   
 $3(6) + y = 20 \quad \boxed{y = 2}$   
 $18 + y = 20 \quad \text{Solution is } (6,2)$

### Solve using Elimination/Addition :

- 1) Determine LCD of one variable's coefficients, or multiply each by the other's coefficient.  
 LCD of  $x$ 's is 6, or multiply 3 by 2, and 2 by 3  
 Make sure one becomes a negative.  
 $2(3x + y = 20) \rightarrow 6x + 2y = 40$   
 $-3(2x + 3y = 18) \rightarrow \underline{-6x - 9y = -54}$   
 $\phantom{-3(2x + 3y = 18) \rightarrow} \phantom{-6x} - 7y = -14$
- 2) Solve for the remaining variable.  
 $\frac{-7y}{-7} = \frac{-14}{-7} \quad \boxed{y = 2}$
- 3) Use this solution in one of the original equations and solve for the other variable.  
 $3x + y = 20$   
 $3x + 2 = 20$   
 $\phantom{3x} - 2 \quad - 2 \quad \boxed{x = 6}$   
 $3x = 18 \quad \text{Solution is } (6,2)$

### Solve using Graphing:

Use table of values or change equations to slope-intercept form.

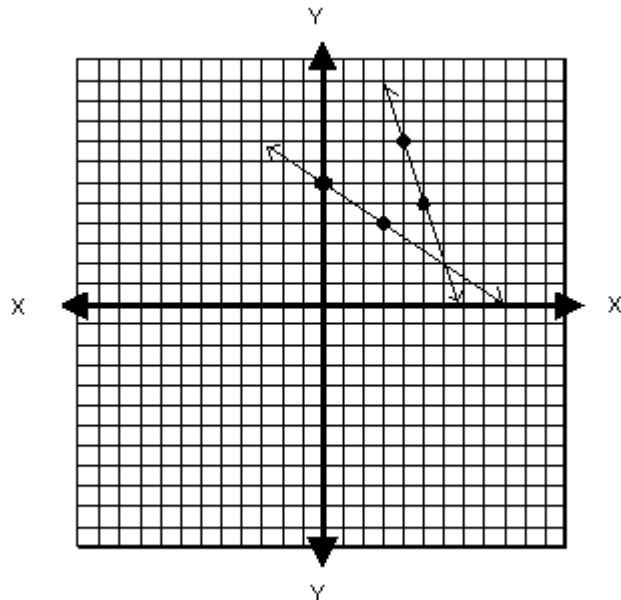
$$3x + y = 20$$

$x$	$y$
4	8
5	5

$$2x + 3y = 18$$

$x$	$y$
0	6
3	4

The lines cross at (6,2)



The solution to the system is: (6,2)